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Geometric Deep Learning on 3D Meshes an overview

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Based on contributions from (among others):

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Who is this aimed at?



The ideal audience

- Limited practical experience with geometrical deep learning
- Has a good understanding of basic convolutional neural networks
 - Has seen the U-net before
- Might come in a situation where your data is actually 3D meshes or have been *magicked* into 3D meshes
- Would like to do surface based classification or labelling / segmentation
- Lacks a good starting point
 - Which approach is good for my data



Solution When poll is active, respond at **pollev.com/rasmuspaulse538**

What is your experience with geometric deep learning?

This is the first time I hear about it

I have superficial knowledge about the field

I have read several articels about it

I have tested an existing framework

I have adapted an existing framework to my own data

I have coded my own framework



What's in it for me?

- You will (hopefully) get an overview of different approaches to work with 3D meshes
 - Some understanding of the strengths and weaknesses of the different methods
 - How invariant the methods are to geometric transformation (translation, rotations etc)
 - How large meshes can they process?
 - What are the restriction with regards to geometry/topology
 - How do they handle noise?







Solution When poll is active, respond at **pollev.com/rasmuspaulse538**

What is my interest in the field?

I am here for the ECTS, the social network and of general interest

I am working with data that might benefit from geometric deep learning

I have a theoretical interest in the field and would like to advance the theory in the field

Something else

Surfaces – where do they come from?



Direct surface scanning using a Canfield Vectra facial scanner.



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Object scanners







An ear impression scanned by a 3Shape scanner.

Probably one of the most scanned anatomies in the world



The founder of DTU – H. C. Ørsted

Scanned by Dolores Messer with a custom built structured light scanner at DTU Compute

Eiríksson et al. "Precision and accuracy parameters in structured light 3-D scanning." International Archives of the Photogrammetry, Remote Sensing and Spatial Information Sciences 5 (2016)



Iso-surfaces or pixel-wise classifications





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CAD Models



Chang, Angel X., et al. "Shapenet: An information-rich 3d model repository." (2015).



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Important properties of meshes

Rotational aspects (geometric invariances)
Size (number of vertices and faces)
Topology and if it is "manifold"
Mesh sampling and noise properties





Translation and rotational aspects



Does it make sense to have a "canonical orientation" of your objects?
Does the method require that the objects are preoriented?



 Translation is often fixed by aligning center-of-mass
 Not a universal solution





Mesh sizes

Туре	Vertices	Faces
Shapenet model (CAD)	Hundreds (guess)	Hundreds (guess)
Facial scan with accuracy~0.5 mm	110.000	35.440
Left atrium from CT scan (voxel size 0.50mm^3) (iso-surface)	35.000	65.000
Scanned H. C. Ørsted (accuracy 150 mikrometer)	1.375.930	2.751.840
Full head model with accuracy ~1 mm	450.000	830.000
FAUST human body (processed)	6.890	



What are the topogogical equivalences of the three meshes?

Sphere, Sphere, Plane

Sphere, Plane, Plane

Sphere, Plane, Tube

Plane, Sphere, Tube

Sphere, Sphere, Sphere

What are the topogogical equivalences of the three meshes?

Sphere, Sphere, Plane

Sphere, Plane, Plane

Sphere, Plane, Tube

Plane, Sphere, Tube

Sphere, Sphere, Sphere



What are the topogogical equivalences of the three meshes?

Sphere, Sphere, Plane

Sphere, Plane, Plane

Sphere, Plane, Tube

Plane, Sphere, Tube

Sphere, Sphere, Sphere



Mesh topology

Topologically equivalent to a - sphere, plane, tube, donut? – or something far far beyond? Is it "manifold" ?



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Venkatesh, Rahul, et al. "DUDE: Deep Unsigned Distance Embeddings for Hi-Fidelity Representation of Complex 3D Surfaces." arXiv:2011.02570 (2020).



Mesh sampling and noise?

- Are the vertices sampled equally over the underlying surface?
- Are the faces/triangles well shaped?
 - Classical marching cubes makes notoriously bad aspect ratio triangles
- What is the nature of the sampling noise?
 - Outliers, Gaussian or something else?









A mesh biopsy



Raw facial scan from BU 3DFE – a reference dataset

- "Mesh in the wild"
 - representative for current facial scanners
- 106.320 vertices and 35.440 faces

"A 3D Facial Expression Database For Facial Behavior Research" by Lijun Yin; Xiaozhou Wei; Yi Sun; Jun Wang; Matthew J. Rosato, 7th International Conference on Automatic Face and Gesture Recognition, 10-12 April 2006 P:211 - 216



A mesh biopsy



- Looks topologically to be a plane
 - but it is not
- Flipped triangles
- Non-manifold parts
- Complex noise issues
- A face has a canonical orientation
 - But facial scanners have many different coordinate systems



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Do topology and artefacts matter?

Quite a lot actually

 A lot of the current methods have severe restrictions on topology and if the surfaces are manifold

A crude comparison

 Imagine your 2D CNN would crash and burn because of one single bad pixel due to a dead CCD cell

A typical solution – preprocess the mesh so it is nice and clean

- Often needs a specific solution for each dataset
- Large risk of removing / smoothing out important information



IN When poll is active, respond at **pollev.com/rasmuspaulse538**

My experience with the U-net

Never heard of it

I have superficial knowledge of the U-net

I have read several papers where the U-net is used

I have tried a pre-made U-net

I have coded my own custom version of the U-net

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CNN recap – the U-net





Convolution – a conceptual heads-up



Approaches covered in the following

- Multi-view rendering approaches
- Volumetric approaches
- Methods that define convolutions on meshes
- Methods based on implicit representations of meshes.
 - For example implicit functions on grids and signed/un-signed distance fields
- Hybrid methods based on mesh operations for convolutions and pooling



Disclaimer: It will mostly be a conceptual overview I am certainly not a specialist on all approaches.



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Multi-view Convolutional Neural Networks for 3D Shape Recognition

Hang Su

Subhransu Maji Evangelos Kalogerakis University of Massachusetts, Amherst Erik Learned-Miller

٠Şe

{hsu,smaji,kalo,elm}@cs.umass.edu

1900 google scholar citations per August 2021



Su, Hang, et al. "Multi-view convolutional neural networks for 3d shape recognition." *Proceedings* of the IEEE international conference on computer vision. 2015.



Multi-view convolutional neural networks for 3d shape recognition



Object classification based on 3D shapes
Rendering pipeline
Standard 2D CNN to do the classification



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12 positions with rotations around the z-axis

- 80 views
 - 20 vertices of an icosahedron enclosing the shape
 - 4 rotations around camera axes



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Multi-view convolutional neural networks for 3d shape recognition – network





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Multi-view convolutional neural networks for 3d shape recognition – results

Princeton ModelNet

- 128K 3D CAD models
- Modelnet40
- 12K models

• 662 categories

• 40 categories

Method	Training Config.			Test Config.	Classification	Retrieval
	Pre-train	Fine-tune	#Views	#Views	(Accuracy)	(mAP)
(1) SPH [16]	-	-	_	-	68.2%	33.3%
(2) LFD [5]	-	-	-	-	75.5%	40.9%
(3) 3D ShapeNets [37]	ModelNet40	ModelNet40	-	-	77.3%	49.2%
(4) FV	-	ModelNet40	12	1	78.8%	37.5%
(5) FV, $12 \times$	-	ModelNet40	12	12	84.8%	43.9%
(6) CNN	ImageNet1K	-	-	1	83.0%	44.1%
(7) CNN, f.t.	ImageNet1K	ModelNet40	12	1	85.1%	61.7%
(8) CNN, 12×	ImageNet1K	-	-	12	87.5%	49.6%
(9) CNN, f.t., $12\times$	ImageNet1K	ModelNet40	12	12	88.6%	62.8%
(10) MVCNN, 12×	ImageNet1K	-	-	12	88.1%	49.4%
(11) MVCNN, f.t., $12 \times$	ImageNet1K	ModelNet40	12	12	89.9%	70.1%
(12) MVCNN, f.t.+metric, $12 \times$	ImageNet1K	ModelNet40	12	12	89.5%	80.2 %
(13) MVCNN, 80×	ImageNet1K	-	80	80	04.3	36.8%
(14) MVCNN, f.t., 80×	ImageNet1K	ModelNet40	80	80	90.1%	70.4%
(15) MVCNN, f.t.+metric, $80 \times$	ImageNet1K	ModelNet40	80	80	90.1%	79.5%

* f.t.=fine-tuning, metric=low-rank Mahalanobis metric learning



Multi-view convolutional neural networks for 3d shape recognition – some observations

- If you can render your object you can classify it
 - Robust to topology variations, large mesh sizes, noise
- Pre-aligning an object to a canonical orientation is illposed
 - the view sequence is somewhat arbitrary
 - Only partially rotationally invariant





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Multi-view CNN for landmark prediction

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Paulsen et al. "Multi-view consensus CNN for 3D facial landmark placement.". Proc. Asian Conference on Computer Vision. (2018)

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3D landmark prediction



- Given a set of rendered faces
- 2D landmark positions are estimated
- A predicted landmark in 2D corresponds to a line in space





What can RANSAC do for me here?

Sample random positions in space for view directions

Render coherent images of skin

Robustly estimate a line crossing avoiding outlier influence

Effectively computing intersection between rays and a triangulated surface



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What can RANSAC do for me here?

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Effectively computing intersection between rays and a triangulated surface


Least squares and RANSAC





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Using trained network on MR data



Trained on the z-buffer / distance map

Works with significant amount of surface noise

http://shapeml.compute.dtu.dk/



Volumetric CNN for object classification - occupancy representation





30 x 30 x 30 occupancy grid

Qi, Charles R., et al. "Volumetric and multi-view cnns for object classification on 3d data." *Proceedings of the IEEE conference on computer vision and pattern recognition*. 2016.

Wu, Zhirong, et al. "3d shapenets: A deep representation for volumetric shapes." *Proceedings of the IEEE conference on computer vision and pattern recognition*. 2015.



Volumetric CNN for object classification





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Volumetric CNN for object classification – some observations

- If you can turn your object solid you can classify it
 Can only handle closed surfaces
- Pre-aligning an object to a canonical orientation is illposed
 - Only partially rotationally invariant
- Massive loss of resolution when using this volumetric representation



Extrinsic vs. intrinsic



Extrinsic



Cao, Wenming, et al. "A comprehensive survey on geometric deep learning." *IEEE Access* 8 (2020): 35929-35949.



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Convolution – a conceptual heads-up





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How many edge neighbours does an edge have in its 1-ring neighbohood?



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Hybrid methods based on mesh operations for convolutions and pooling



- MeshCNN used for semantic segmentation of 3D objects.
- The labelling is done per edge
- To the left the result of the segmentation
- Second, third and fourth row show simplified/reduced/pooled meshes

https://ranahanocka.github.io/MeshCNN/

Hanocka, Rana, et al. "Meshcnn: a network with an edge." *ACM Transactions on Graphics (TOG)* 38.4 (2019): 1-12.



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b

e

a

MeshCNN – node (edge) data (features)



- The dihedral angle
- The two inner angles
- The two edge-length ratios

Neighborhood of edge e

Invariant to translation, scaling and rotation

$$(\mathbf{e_1},\mathbf{e_2},\mathbf{e_3},\mathbf{e_4})=(\mathbf{a}+\mathbf{c},\mathbf{b}+\mathbf{d},|\mathbf{a}-\mathbf{c}|,|\mathbf{b}-\mathbf{d}|)$$



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MeshCNN – convolutions



 Symmetric features on 1-ring neighbors
 Normal features for edge itself, e₀
 1 x 5 standard 2D convolutions

$$(\mathbf{e_1}, \mathbf{e_2}, \mathbf{e_3}, \mathbf{e_4}) = (\mathbf{a} + \mathbf{c}, \mathbf{b} + \mathbf{d}, |\mathbf{a} - \mathbf{c}|, |\mathbf{b} - \mathbf{d}|)$$





MeshCNN – pooling / unpooling

- The edge with the feature vector of lowest magnitude is collapsed – similar to standard mesh decimation
 Five edges → Two edges
- Bookkeeping matrix G (size #edge x #edge)





MeshCNN – network architectures

Segmentation (Down)

ResConv $f_{in} \times 32$ MeshPool $\rightarrow 1800$ ResConv 32×64 MeshPool $\rightarrow 1350$ ResConv 64×128 MeshPool $\rightarrow 600$ ResConv 128×256

Symmetric up- and down path





MeshCNN with U-net architecture Based on BSc work of Bjørn Marius Schreblowski Hansen & Mathias Micheelsen Lowes





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MeshCNN - results

-	Classif	*		
Γ	Method	Split 16	Split 10]
ſ	MeshCNN	98.6 %	91.0 %	1
Γ	GWCNN	96.6%	90.3%	1)
	GI	96.6%	88.6%	[[Emp. et al. 2017]
	SN	48.4%	52.7%	$\int [Lzuz et al. 2017]$
L	SG	70.8%	62.6%	J



	Human Bo	dy Segmenta	tion	
Î	Method	# Features	Accuracy	
	MeshCNN	5	92.30 %	1
	SNGC	3	91.02%	
	Toric Cover	26	88.00%	
	PointNet++	3	90.77%	
	DynGraphCNN	3	89.72%	[2018]
	GCNN	64	86.40%	
	MDGCNN	64	89.47%	



https://ranahanocka.github.io/MeshCNN/

Hanocka, Rana, et al. "Meshcnn: a network with an edge." *ACM Transactions on Graphics (TOG)* 38.4 (2019): 1-12.



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MeshCNN - observations

- Achieved impressive segmentation results on standard datasets
 - Invariant to rotation, scaling and translation
- Limited to small meshes with a few hundred edges
 - Due to N^2 memory foot prints (in matrix G)
- Vulnerable to mesh topology and surfaces being manifold
 - Can create non-manifold surfaces during pooling





Sparse MeshCNN with attentation paper in review

Based on BSc work of Bjørn Marius Schreblowski Hansen & Mathias Micheelsen Lowes



Prediction of intersection between the left atrium and the left atrial appendage in the human heart. For simulation of surgical device insertion.



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Sparse MeshCNN

- In MeshCNN
 - The matrix **G** is of size n_e^2
 - Scales quadratically with mesh size
- In Sparse MeshCNN
 - The matrix **G** is sparse
 - Can operate on larger meshes





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Methods based on convolutions on meshes

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Pv	Torch
	geometric

latest

Search docs

- Installation
- Introduction by Example
- Creating Message Passing Networks
- **Creating Your Own Datasets**
- Advanced Mini-Batching
- Memory-Efficient Aggregations
- TorchScript Support
- **GNN** Cheatsheet
- Colab Notebooks
- External Resources

PACKAGE REFERENCE

- torch_geometric
- □ torch_geometric.nn
- **Convolutional Layers**
- Dense Convolutional Layers
- Normalization Layers
- **Global Pooling Layers**
- Pooling Layers
- **Dense Pooling Layers**
- Unpooling Layers
- Models
- Functional
- DataParallel Layers
- torch_geometric.data
- torch_geometric.datasets
- torch_geometric.transforms
- torch_geometric.utils
- torch_geometric.io

Convolutiona	al Lavers	MFConv
	,	RGCNConv
MessagePassing	Base class for creating message passing layers of the form	FastRGCN
GCNConv	The graph convolutional operator from the "Semi-supervised Classification with Graph Convolutional Networks" paper	SignedCo
ChebConv	The chebyshev spectral graph convolutional operator from the "Convolutional Neural Networks on Graphs with Fast Localized Spectral Filtering" paper	DNAConv
SAGEConv	The GraphSAGE operator from the "Inductive Representation Learning on Large Graphs" paper	PointNet
GraphConv	The graph neural network operator from the "Weisfeiler and Leman Go Neural:	GMMConv
	Higher-order Graph Neural Networks paper	SplineCo
GravNetConv	The GravNet operator from the "Learning Representations of Irregular Particle- detector Geometry with Distance-weighted Graph Networks" paper, where the graph is dynamically constructed using nearest neighbors.	NNConv
	The gated graph convolution operator from the "Gated Graph Sequence Neural	ECConv
GatedGraphConv	Networks" paper	CGConv
ResGatedGraphConv	The residual gated graph convolutional operator from the "Residual Gated Graph ConvNets" paper	EdgeConv
GATConv	The graph attentional operator from the "Graph Attention Networks" paper	DynamicE
GATv2Conv	The GATv2 operator from the "How Attentive are Graph Attention Networks?" paper, which fixes the static attention problem of the standard GATCONV layer: since the linear layers in the standard GAT are applied right after each other, the ranking of attended nodes is unconditioned on the query node.	XConv
TransformerConv	The graph transformer operator from the "Masked Label Prediction: Unified Message Passing Model for Semi-Supervised Classification" paper	FeaStCon
AGNNConv	The graph attentional propagation layer from the "Attention-based Graph Neural Network for Semi-Supervised Learning" paper	Hypergra
TAGConv	The topology adaptive graph convolutional networks operator from the "Topology Adaptive Graph Convolutional Networks" paper	PNAConv
GINConv	The graph isomorphism operator from the "How Powerful are Graph Neural Networks?" paper	ClusterG
GINEConv	The modified GINCONV operator from the "Strategies for Pre-training Graph Neural	GENConv
		GCN2Conv
ARMAConv	The ARMA graph convolutional operator from the "Graph Neural Networks with Convolutional ARMA Filters" paper	PANConv
SGConv	The simple graph convolutional operator from the "Simplifying Graph Convolutional Networks" paper	WLConv
		FiLMConv

The approximate personalized propagation of neural predictions layer from the "Predict then Propagate: Graph Neural Networks meet Personalized PageRank" paper

MFConv	for Learning Molecular Fingerprints" paper
RGCNConv	The relational graph convolutional operator from the "Modeling Relational Data with Graph Convolutional Networks" paper
FastRGCNConv	See rgCNConv .
SignedConv	The signed graph convolutional operator from the "Signed Graph Convolutional Network" paper
DNAConv	The dynamic neighborhood aggregation operator from the "Just Jump: Towards Dynamic Neighborhood Aggregation in Graph Neural Networks" paper
PointNetConv	The PointNet set layer from the "PointNet: Deep Learning on Point Sets for 3D Classification and Segmentation" and "PointNet++: Deep Hierarchical Feature Learning on Point Sets in a Metric Space" papers
PointConv	alias Of torch_geometric.nn.conv.point_conv.PointNetConv
GMMConv	The gaussian mixture model convolutional operator from the "Geometric Deep Learning on Graphs and Manifolds using Mixture Model CNNs" paper
SplineConv	The spline-based convolutional operator from the "SplineCNN: Fast Geometric Deep Learning with Continuous B-Spline Kernels" paper
NNConv	The continuous kernel-based convolutional operator from the "Neural Message Passing for Quantum Chemistry" paper.
ECConv	alias Of torch_geometric.nn.comv.nn_comv.NNConv
CGConv	The crystal graph convolutional operator from the "Crystal Graph Convolutional Neural Networks for an Accurate and Interpretable Prediction of Material Properties" paper
EdgeConv	The edge convolutional operator from the "Dynamic Graph CNN for Learning on Point Clouds" paper
DynamicEdgeConv	The dynamic edge convolutional operator from the "Dynamic Graph CNN for Learning on Point Clouds" paper (see torch_geometric.mn.com.tdgeCom), where the graph is dynamically constructed using nearest neighbors in the feature space.
XConv	The convolutional operator on $\mathcal X\text{-}transformed$ points from the "PointCNN: Convolution On X-Transformed Points" paper
PPFConv	The PPFNet operator from the "PPFNet: Global Context Aware Local Features for Robust 3D Point Matching" paper
FeaStConv	The (translation-invariant) feature-steered convolutional operator from the "FeaStNet: Feature-Steered Graph Convolutions for 3D Shape Analysis" paper
HypergraphConv	The hypergraph convolutional operator from the "Hypergraph Convolution and Hypergraph Attention" paper
LEConv	The local extremum graph neural network operator from the "ASAP: Adaptive Structure Aware Pooling for Learning Hierarchical Graph Representations" paper, which finds the importance of nodes with respect to their neighbors using the difference operator:
PNAConv	The Principal Neighbourhood Aggregation graph convolution operator from the "Principal Neighbourhood Aggregation for Graph Nets" paper
ClusterGCNConv	The ClusterGCN graph convolutional operator from the "Cluster-GCN: An Efficient Algorithm for Training Deep and Large Graph Convolutional Networks" paper
GENConv	The GENeralized Graph Convolution (GENConv) from the "DeeperGCN: All You Need to Train Deeper GCNs" paper.
GCN2Conv	The graph convolutional operator with initial residual connections and identity mapping (GCNII) from the "Simple and Deep Graph Convolutional Networks" paper
PANConv	The path integral based convolutional operator from the "Path Integral Based Convolution and Pooling for Graph Neural Networks" paper
WLConv	The Weisfeiler Lehman operator from the "A Reduction of a Graph to a Canonical Form and an Algebra Arising During this Reduction" paper, which iteratively refines node colorings:
FiLMConv	The FiLM graph convolutional operator from the "GNN-FiLM: Graph Neural Networks with Feature-wise Linear Modulation" paper
	The self-supervised graph attentional operator from the "How to Find Your Friendly

Neighborhood: Graph Attention Design with Self-Supervision" paper

SuperGATConv

APPNP



Pooling Layers

TopKPooling	$top_{\rm k}$ pooling operator from the "Graph U-Nets", "Towards Sparse Hierarchical Graph Classifiers" and "Understanding Attention and Generalization in Graph Neural Networks" papers
SAGPooling	The self-attention pooling operator from the "Self-Attention Graph Pooling" and "Understanding Attention and Generalization in Graph Neural Networks" papers
EdgePooling	The edge pooling operator from the "Towards Graph Pooling by Edge Contraction" and "Edge Contraction Pooling for Graph Neural Networks" papers.
ASAPooling	The Adaptive Structure Aware Pooling operator from the "ASAP: Adaptive Structure Aware Pooling for Learning Hierarchical Graph Representations" paper.
PANPooling	The path integral based pooling operator from the "Path Integral Based Convolution and Pooling for Graph Neural Networks" paper.
MemPooling	Memory based pooling layer from "Memory-Based Graph Networks" paper, which learns a coarsened graph representation based on soft cluster assignments
max_pool	Pools and coarsens a graph given by the torch_geometric.data.Data object according to the clustering defined in cluster .
avg_pool	Pools and coarsens a graph given by the torch_geometric.data.Data Object according to the clustering defined in cluster .
max_pool_x	Max-Pools node features according to the clustering defined in $\ {\tt cluster}$.
max_pool_neighbor_x	Max pools neighboring node features, where each feature in $data.x$ is replaced by the feature value with the maximum value from the central node and its neighbors.
avg_pool_x	Average pools node features according to the clustering defined in $\ _{\mbox{cluster}}$.
<pre>avg_pool_neighbor_x</pre>	Average pools neighboring node features, where each feature in data.x is replaced by the average feature values from the central node and its neighbors.
graclus	A greedy clustering algorithm from the "Weighted Graph Cuts without Eigenvectors: A Multilevel Approach" paper of picking an unmarked vertex and matching it with one of its unmarked neighbors (that maximizes its edge weight).
voxel_grid	Voxel grid pooling from the, e.g., Dynamic Edge-Conditioned Filters in Convolutional Networks on Graphs paper, which overlays a regular grid of user- defined size over a point cloud and clusters all points within the same voxel.
fps	A sampling algorithm from the "PointNet++: Deep Hierarchical Feature Learning on Point Sets in a Metric Space" paper, which iteratively samples the most distant point with regard to the rest points.
knn	Finds for each element in $\ _{y}$ the $\ _{k}$ nearest points in $\ _{x}$.
knn_graph	Computes graph edges to the nearest κ points.
radius	Finds for each element in $\ _{y}$ all points in $\ _{x}$ within distance $\ _{r}$.
radius_graph	Computes graph edges to all points within a given distance.
nearest	Clusters points in $\ \star \$ together which are nearest to a given query point in $\ _{y}$.



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Convolutions on meshes

		$\pi/2$ $5\pi/6$ $7\pi/6$ $4\pi/3$ $3\pi/2$	$\pi/3$ $4\pi/4$ $\pi/6$ $5\pi/6$ $\pi/6$ $5\pi/3$ $7\pi/6$ $7\pi/6$ $4\pi/3$	$\pi/2$ $\pi/3$ $\pi/6$	$5\pi/6$ $7\pi/6$ $4\pi/3$	$\pi/2$ $\pi/3$ $\pi/6$ 0 0 0 0 0 1 $1\pi/6$ $3\pi/2$ $5\pi/3$
Polar coor	rdinates ρ, θ	GCNN		ACNN		MoNet
		Monti et al., Geometric deep	learning on graphs and manifolds usir	ig mixture model CNNs, 2017, CVPR		-
		$(D(x)f)(\rho,\theta) = \int_{X} v_{\rho,\theta} \left(x \right)^{-1} dx$	$(D_{\alpha}(x)f)(x') dx'$ $(D_{\alpha}(x)f)(x)$	$\theta, t) = \frac{\int_{\mathbf{X}} h_{\alpha\theta_t}(x, x') f(x') dx'}{\int_{\mathbf{X}} h_{\alpha\theta_t}(x, x') dx'}$	$D_j(x)f =$	$= \sum_{x \in N(x)} w_j \left(\mathbf{u} \left(x, x' \right) \right) f(x')$
		$(f * g)(x) = \max_{\Delta \theta \in [0, 2\pi)} \int_0^{2\pi} \int_0^{\rho_{\max}}$	$g(\rho, \theta + \Delta \theta) \qquad (f * g) (a, \theta) = (D(x)f)(\rho, \theta)d\rho d\theta$	$\mathbf{x}) = \int g\left(\theta, t\right) \left(D_{\alpha}\left(x\right)f\right)\left(\theta, t\right) d\mathbf{x}$	$dtd\theta$ $(f*g)$	$f(x) = \sum_{j=1}^{J} g_j D_j(x) f$
	Method	Pseudo-coordinates	$\mathbf{u}(x,y)$	Weight function $w_j(\mathbf{u}), j =$	$1,\ldots,J$	
	CNN [23]	Local Euclidean	$\mathbf{x}(x,y) = \mathbf{x}(y) - \mathbf{x}(x)$	$\delta(\mathbf{u}-ar{\mathbf{u}}_j)$,	
	GCNN [26]	Local polar geodesic	$\rho(x,y), \theta(x,y)$	$\exp\left(-\frac{1}{2}(\mathbf{u}-\bar{\mathbf{u}}_j)^{\top}\begin{pmatrix}\bar{\sigma}_{\rho}^2\\\bar{\sigma}_{\alpha}^2\end{pmatrix}\right)$	$(\mathbf{u} - \bar{\mathbf{u}}_j))$	
	ACNN [7]	Local polar geodesic	$\rho(x,y), \theta(x,y)$	$\exp\left(-\frac{1}{2}\mathbf{u}^{T}\mathbf{R}_{\bar{\theta}_{j}}\left(\begin{smallmatrix}\bar{\alpha}\\1\end{smallmatrix}\right)\mathbf{R}_{\bar{\theta}_{j}}^{T}\mathbf{u}\right)$)	
	GCN [21]	Vertex degree	$\deg(x), \deg(y)$	$\left(1 - \left 1 - \frac{1}{\sqrt{u_1}}\right \right) \left(1 - \left 1 - \frac{1}{\sqrt{u_1}}\right \right)$	$\frac{1}{\sqrt{u_2}} $	
	DCNN [3]	Transition probability in r hops	$p^0(x,y),\ldots,p^{r-1}(x,y)$	$\operatorname{id}(u_j)$		

Cao, Wenming, et al. "A comprehensive survey on geometric deep learning." *IEEE Access* 8 (2020): 35929-35949.





Convolution – a conceptual heads-up





Convolutions on meshes



Main differences between approaches

- How is a node neighborhood defined / computed
- What values are used per node
- How are the weights in the convolutions defined

 How are we dealing with kernel rotational invariance?

Cao, Wenming, et al. "A comprehensive survey on geometric deep learning." *IEEE Access* 8 (2020): 35929-35949.

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One example - MoNet



Monti, F., Boscaini, D., Masci, J., Rodola, E., Svoboda, J., & Bronstein, M. M. (2017). Geometric deep learning on graphs and manifolds using mixture model CNNs. *Proc.CVPR*.





MoNet – vertex features



Fig. 4. Signature structure for SHOT Vertex features should represent local geometry
Local shape signature

Histogram of local normal vectors

- 544 dimensional vector (per vertex)

Tombari et al. "Unique signatures of histograms for local surface description." *European conference on computer vision*. 2010.

Monti, F., Boscaini, D., Masci, J., Rodola, E., Svoboda, J., & Bronstein, M. M. (2017). Geometric deep learning on graphs and manifolds using mixture model CNNs. *Proc.CVPR*.



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MoNet – vertex features. Bam! Back to classical shape matching



Fig. 4. Signature structure for SHOT

IEEE TRANSACTIONS ON PATTERN ANALYSIS AND MACHINE INTELLIGENCE, VOL. 24, NO. 24, APRIL 2002

Shape Matching and Object Recognition Using Shape Contexts





Serge Belongie, Member, IEEE, Jitendra Malik, Member, IEEE, and Jan Puzicha







The local shape descriptor used in MoNet is similar to 3D extensions of shape contexts – and comes with its own choices, strengths and weaknesses.

Tombari et al. "Unique signatures of histograms for local surface description." *European conference on computer vision*. 2010.



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Local reference frame







- The local reference frame is the per-vertex coordinate system
- Determines the orientation of SHOT feature extractor
- Might determine the orientation of the local convolution patch
 - Unless convolution is taken as the maximum over all rotations (around the normal) of the patch





Inconsistent local reference frame

•		•	•	•	•
lacksquare	lacksquare	lacksquare		•	
•	ullet		ullet	ullet	\bullet
ullet					\bullet
ullet	lacksquare	•		۲	lacksquare
ullet			•	lacksquare	ullet

- Imagine that you had no general orientation of your 2D image
- For each pixel, your convolution kernel has an arbitrary orientation
- That is the default situation with 3D meshes







Inconsistent local reference frame

- One approach:
 - Compute local reference frame (coordinate system) following the gradient in the image
 - Convolutions would be following gradients maybe good maybe bad
- Another approach: Rotate kernel and take the maximum output...very expensive







Computing a Local reference frame - using a 3D equivalent of gradients/curvature





Sample points in a local neighborhood

- Do eigenvector decomposition
- 3 Eigenvectors
 - One is the normal (smallest eigenvalue)
 - Two follow the surface
- Normally inconsistent and ambiguous
- Reference below claims to have solved it
- Used in MoNet (as far as I understand the paper)

Tombari et al. "Unique signatures of histograms for local surface description." *European conference on computer vision*. 2010.



MoNet and similar methods – observations



Choice of local features to represent geometry
 Are they dependent on a consistent local reference frame?
 Topological constraints?

Monti, F., Boscaini, D., Masci, J., Rodola, E., Svoboda, J., & Bronstein, M. M. (2017). Geometric deep learning on graphs and manifolds using mixture model CNNs. *Proc.CVPR*.





A note on spectral methods

- There is a strong relation between Fourier analysis and convolutions for 1D and 2D signals
- This can be replicated on 3D meshes and is also related to the mesh Laplacian
- Quite a lot of spectral methods have been published
- It seems that the are loosing popularity and they are beyond the scope and time of this presentation
- Some comments can be found in
 - Monti, F., Boscaini, D., Masci, J., Rodola, E., Svoboda, J., & Bronstein, M. M. (2017). Geometric deep learning on graphs and manifolds using mixture model CNNs. Proc.CVPR.





Deep learning with implicit functions The signed distance function



- Voxel grid each voxel contains a scalar value
- Carries information about the shape in the entire field


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Park, Jeong Joon, et al. "Deepsdf: Learning continuous signed distance functions for shape representation." *Proc. Computer Vision and Pattern Recognition*. 2019.



DeepSDF – single shape representation

Single shape representation

$$f(p) \mapsto s, \qquad p \in \mathbb{R}^3, s \in \mathbb{R}^3$$









DeepSDF – multiple shape representation

Multiple shape representation









DeepSDF - Training





DeepSDF - results

Results:

- Reconstructing known shapes
- Reconstructing unknown shapes
- Shape completion
- Latent space shape interpolation





Figure 1: DeepSDF represents signed distance functions (SDFs) of shapes via latent code-conditioned feed-forward decoder networks. Above images are raycast renderings of DeepSDF interpolating between two shapes in the learned shape latent space. Best viewed digitally.







(b) Completion (ours)





DeepSDF - observations

- You should be able compute a signed distance to your mesh
 - Needs closed surfaces
- Not rotational invariant unless you do heavy data augmentation
- Can do shape classification, shape synthesis and shape completion
 - Has a very usable latent space





Other implicit approaches

Implicit Functions in Feature Space for 3D Shape Reconstruction and Completion

Julian Chibane^{1,2}

Thiemo Alldieck^{1,3} Gerard Pons-Moll¹

¹Max Planck Institute for Informatics, Saarland Informatics Campus, Germany ²University of Würzburg, Germany ³Computer Graphics Lab, TU Braunschweig, Germany {jchibane, gpons}@mpi-inf.mpg.de alldieck@cg.cs.tu-bs.de



Adversarial Generation of Continuous Implicit Shape Representations

Marian Kleineberg, Matthias Fey and Frank Weichert

TU Dortmund University, Germany



SAL: Sign Agnostic Learning of Shapes from Raw Data

Matan Atzmon and Yaron Lipman Weizmann Institute of Science Rehovot, Israel







Unsigned distance fields



Implicit Neural Distance Representation for Unsupervised and Supervised Classification of Complex Anatomies. *Kristine Aavild Juhl et al.* **MICCAI 2021**

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Unsigned distance fields

Can handle arbitrary topologiesMeshing an unsigned distance field is very tricky



Implicit Neural Distance Representation for Unsupervised and Supervised Classification of Complex Anatomies. *Kristine Aavild Juhl et al.* **MICCAI 2021**



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Shape classification using unsigned distance fields

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Fig. 3. Visualization of the latent space projected to 2D using principle component analysis (PCA) for the 128 dimensional latent space of the three datasets (left) and the ESOF-faces only (right). Opaque: training set, Solid: test set.



Implicit Neural Distance Representation for Unsupervised and Supervised Classification of Complex Anatomies. *Kristine Aavild Juhl et al.* **MICCAI 2021**

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That's is – the tour is over!



If you have data and need a way forward

What is the nature of my data?

- number of samples, number of vertices, topology, cleanness, canonical orientations?
- What is my goal?
 - segmentation, classification, shape correspondence, shape completion?
- What approach fits my data and goals?
 - can it handle your data (size is a main issue)
 - can it be adapted to solve your task?
 - are there any code available
 - what are the hardware requirements (mainly GPU memory size)
 - what are the software / operating system requirements?



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What if I need a more theoretical research direction?

- Find your own niche that you want to explore
- Locate an unsolved problem
- In GDL there are lots of problems
 - but also a large of number of people looking at them.
- You should have a competitive advantage
 - new idea, alternative approaches

A new mesh convolution operator will probably have limited novelty



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